| | |
|---|---|
| Instructor: | Frank Secretain |
| Course: | Math 1004 |
| Date: | September 30, 2025 |
| | |
| Assessment: | Test 1 |
| Time allowed: | 110 minutes |
| Devices allowed: | Pencil, pen, eraser, calculator |
| Notes from instructor: | Be neat.  Show your work where needed.  Box final answers. |
| | |
| Marks allocated: | 5 questions worth 20 marks |
| Percentage of final grade: | 20% of final grade |

# Formula Sheet

## Order of Operations

$$ac + bc = c(a + b)$$

### exponents

$$a^n a^m = a^{n+m}$$

$$(a^n)^m = a^{nm}$$

$$(ab)^n = a^n b^n$$

$$a^0 = 1$$

$$a^{-n} = \frac{1}{a^n}$$

### radicals

$$a^{\frac{n}{m}} = \sqrt[m]{a^n}$$

## Relative Velocity

$$\vec{v}_{\frac{A}{C}} = \vec{v}_{\frac{A}{B}} + \vec{v}_{\frac{B}{C}}$$

## Linear equations (Cramer's rule)

$$x_i = \frac{det(A_i)}{det(A)}$$

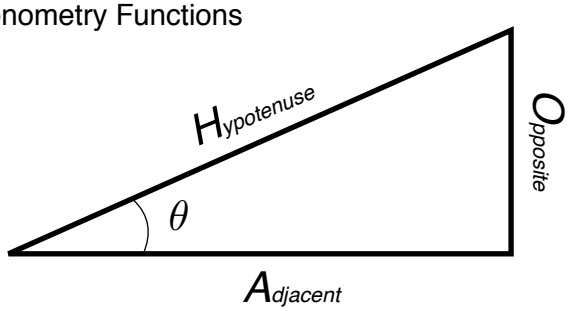
## Forms of a 2nd order polynomial

$$y = ax^2 + bx + c$$

$$y = a(x - h)^2 + k$$

$$y = (x - m)(x - n)$$

## Trigonometry Functions




$$sin(\theta) = \frac{O}{H} \qquad sin^{-1}\left(\frac{O}{H}\right) = \theta$$

$$cos(\theta) = \frac{A}{H} \qquad cos^{-1}\left(\frac{A}{H}\right) = \theta$$

$$tan(\theta) = \frac{O}{A} \qquad tan^{-1}\left(\frac{O}{A}\right) = \theta$$

## Pythagoras Theorem

$$H^2 = O^2 + A^2$$

## Unit Conversions

### angles

$$2\pi = 6.28 \text{ rad} = 360^o$$

### mass

$$1 \text{ kg} = 2.2 \text{ lbs.}$$

### lengths

$$1 \text{ mile} = 1.6 \text{ km}$$

$$1 \text{ inch} = 2.54 \text{ cm}$$

$$1 \text{ m} = 3.3 \text{ ft}$$

### volumes

$$1 \text{ gallon} = 3.78 \text{ Litres}$$

(4 marks) Match the “type of number” with the best “example number”. Draw a line to match the “type of number” to the “example number” to indicate your answer.

| | |
|---|---|
| irrational | $+2$ |
| integer | $\sqrt{2}$ |
| rational | $-2$ |
| whole | $-2.2$ |

(3 marks) Determine

a) the total number of significant digits and
b) the number of decimal places to the least significant digit
c) re-write the number in scientific notation

for the following number:

0.01320

a) significant digits = _____

b) decimal places = _____

c) scientific notation = _____

(3 marks) Solve the each expression and keep the correct number of significant digits.

2200+178.183

(10.0)(0.7240)

239.76+(6810)(1.72691)

(5 marks) Given the standard unit conversion table on the formula sheet (1st page), convert each of the numbers to the stated units.

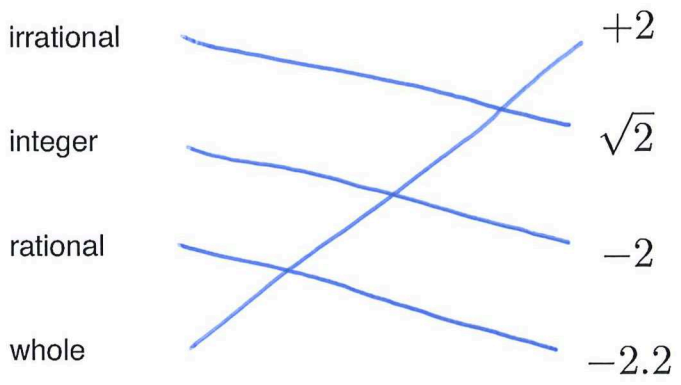
$$5.2\ \frac{\text{lbs.}}{\text{minute}} \rightarrow\ \frac{\text{kg}}{\text{second}}$$

$$0.0134\ \frac{\text{degrees}}{\text{second}} \rightarrow\ \frac{\text{radians}}{\text{hour}}$$

$$0.983\ \frac{\text{gallon}^2}{\text{second}} \rightarrow \frac{\text{Litre}^2}{\text{second}}$$

(5 marks) You run 810 m East, 250 m North and 220 m at $40^0$ West of North. How far are you from where you started?

(4 marks) Match the "type of number" with the best "example number". Draw a line to match the "type of number" to the "example number" to indicate your answer.




(3 marks) Determine

a) the total number of significant digits and
b) the number of decimal places to the least significant digit
c) re-write the number in scientific notation

for the following number:

0.01320 (+5)

a) significant digits = 4

b) decimal places = +5

c) scientific notation = $1.320 \times 10^{-2}$

(3 marks) Solve the each expression and keep the correct number of significant digits.

$2200 + 178.183 = 2378.183$ (-2, +3, -2)

$= \boxed{2400}$

$(10.0)(0.7240) = 7.240$ (3, 4)

$= \boxed{7.24}$

$239.76+\underbrace{(6810)}_{3}\underbrace{(1.72691)}_{6} = 239.\underbrace{76}_{+2} + 11\underbrace{760}_{-2}.2571$

$= 12\underbrace{000}_{-2}.0171$

$= \boxed{1.20 \times 10^4}$

(5 marks) Given the standard unit conversion table on the formula sheet (1st page), convert each of the numbers to the stated units.

$$5.2 \ \frac{\text{lbs.}}{\text{minute}} \rightarrow \frac{\text{kg}}{\text{second}}$$

$$5.2 \ \frac{\cancel{\text{lbs}}}{\cancel{\text{min}}}\left(\frac{1\ \text{kg}}{2.2\cancel{\text{lbs}}}\right)\left(\frac{1\ \cancel{\text{min}}}{60\ \text{sec}}\right) = \boxed{0.039\ \frac{\text{kg}}{\text{sec}}}$$

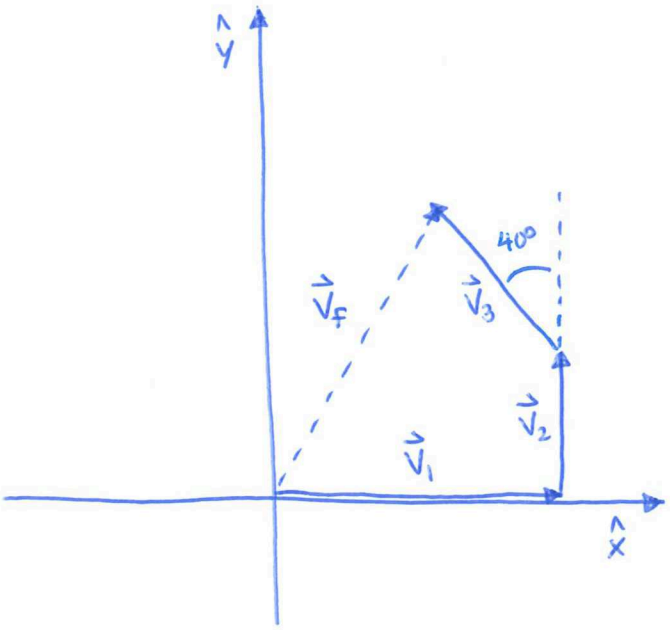
$$0.0134 \ \frac{\text{degrees}}{\text{second}} \rightarrow \frac{\text{radians}}{\text{hour}}$$

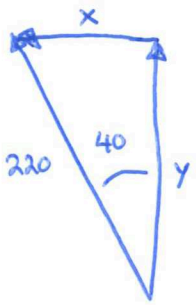
$$0.0134 \ \frac{\cancel{\text{deg}}}{\cancel{\text{sec}}}\left(\frac{2\pi\ \text{rad}}{360\ \cancel{\text{deg}}}\right)\left(\frac{60\ \cancel{\text{sec}}}{1\ \cancel{\text{min}}}\right)\left(\frac{60\ \cancel{\text{min}}}{1\ \text{hour}}\right) = \boxed{0.842\ \frac{\text{rads}}{\text{hour}}}$$

$$0.983 \ \frac{\text{gallon}^2}{\text{second}} \rightarrow \frac{\text{Litre}^2}{\text{second}}$$

$$0.983 \ \frac{\cancel{\text{gal}^2}}{\text{sec}}\left(\frac{3.78\,\text{L}}{1\ \cancel{\text{gal}}}\right)\left(\frac{3.78\,\text{L}}{1\ \cancel{\text{gal}}}\right) = \boxed{14.0\ \frac{\text{L}^2}{\text{sec}}}$$

(5 marks) You run 810 m East, 250 m North and 220 m at 40⁰ West of North. How far are you from where you started?




$x = 220 \sin(40)$
$= 141.41$

$y = 220 \cos(40)$
$= 168.53$

$$\vec{V}_1 = 810\,\hat{x} + 0\,\hat{y}$$
$$\vec{V}_2 = 0\,\hat{x} + 250\,\hat{y}$$
$$+\ \vec{V}_3 = -141.41\,\hat{x} + 168.53\,\hat{y}$$
$$\vec{V}_f = 668.59\,\hat{x} + 418.53\,\hat{y}$$

$$|\vec{V}_f| = \sqrt{(668.59)^2 + (418.53)^2}$$

$$= 788.78$$

$$\boxed{|\vec{V}_f| = 789 \text{ m}}$$

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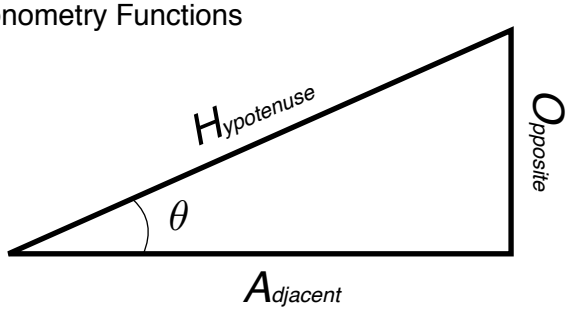


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| integer | $\sqrt{2}$ |
| rational | $-2$ |
| natural | $-2.2$ |

(3 marks) Determine

a) the total number of significant digits and
b) the number of decimal places to the least significant digit
c) re-write the number in scientific notation

for the following number:

0.01020

a) significant digits = _____

b) decimal places = _____

c) scientific notation = _____

(3 marks) Solve the each expression and keep the correct number of significant digits.

2500+170.183

(10.0)(0.7400)

239.76+(6810)(1.72691)

(5 marks) Given the standard unit conversion table on the formula sheet (1st page), convert each of the numbers to the stated units.

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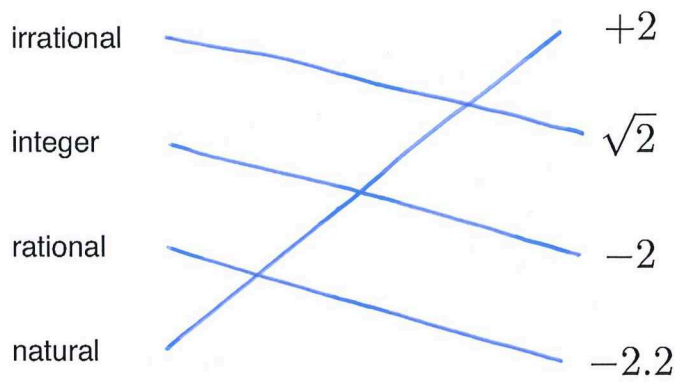
$$0.0134\ \frac{\text{degrees}}{\text{second}} \rightarrow\ \frac{\text{radians}}{\text{hour}}$$

$$0.983\ \frac{\text{gallon}^2}{\text{second}} \rightarrow \frac{\text{Litre}^2}{\text{second}}$$

(5 marks) You run 510 m East, 350 m North and 270 m at $60^0$ West of North. How far are you from where you started?

(4 marks) Match the "type of number" with the best "example number". Draw a line to match the "type of number" to the "example number" to indicate your answer.




(3 marks) Determine

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c) re-write the number in scientific notation

for the following number:

0.01020
+5

a) significant digits = 4

b) decimal places = +5

c) scientific notation = $1.020 \times 10^{-2}$

(3 marks) Solve the each expression and keep the correct number of significant digits.

2500 + 170.183
-2 +3

$= 2670.183$
-2

$= \boxed{2700}$

(10.0)(0.7400)
3 4

$= 7.400$
3

$= \boxed{7.40}$

$239.76+(6810)(1.72691) = 239.76 + 11760.2571$

(3 sig figs) (6 sig figs) (+2) (-2)

$= 12000.0171$

$= \boxed{1.20 \times 10^4}$

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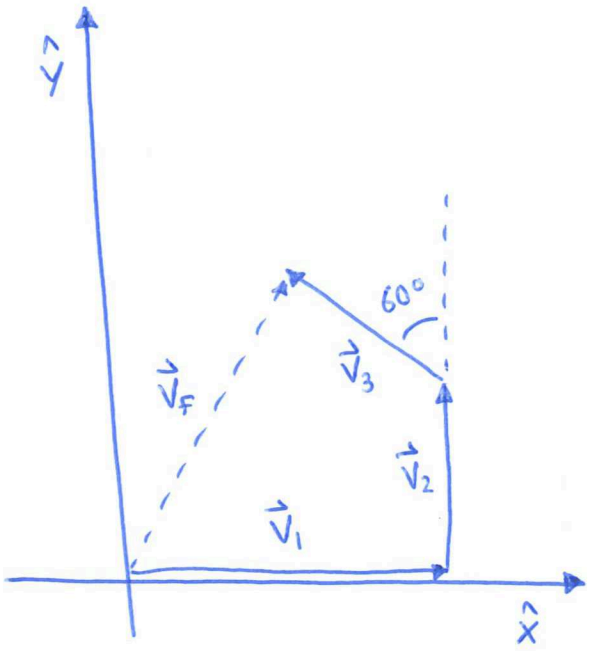
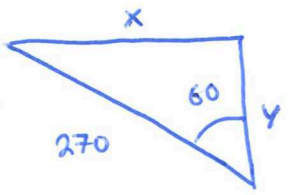
(5 marks) You run 510 m East, 350 m North and 270 m at 60° West of North. How far are you from where you started?




$x = 270 \sin(60)$
$= 233.83$

$y = 270 \cos(60)$
$= 135$

$$\vec{V}_1 = 510\,\hat{x} + 0\,\hat{y}$$
$$\vec{V}_2 = 0\,\hat{x} + 350\,\hat{y}$$
$$+\ \vec{V}_3 = -233.83\,\hat{x} + 135\,\hat{y}$$
$$\vec{V}_f = 276.17\,\hat{x} + 485\,\hat{y}$$

$$|\vec{V}_f| = \sqrt{(276.17)^2 + (485)^2}$$

$$= 558.12$$

$$\boxed{|\vec{V}_f| = 558 \text{ m}}$$