

Instructor: Frank Secretain  
Course: Math 150  
Date: May 26, 2025

Assessment: Test 1  
Time allowed: 110 minutes  
Devices allowed: Pencil, pen, eraser, calculator  
Notes from instructor: Be neat. Show your work where needed. Box final answers.

Marks allocated: 4 questions worth 25 marks  
Percentage of final grade: 25% of final grade

## Formula Sheet

### Order of Operations

$$ac + bc = c(a + b)$$

exponents

$$a^n a^m = a^{n+m}$$

$$(a^n)^m = a^{nm}$$

$$(ab)^n = a^n b^n$$

$$a^0 = 1$$

$$a^{-n} = \frac{1}{a^n}$$

radicals

$$a^{\frac{n}{m}} = \sqrt[m]{a^n}$$

### Relative Velocity

$$\vec{v}_{\frac{A}{C}} = \vec{v}_{\frac{A}{B}} + \vec{v}_{\frac{B}{C}}$$

Linear equations (Cramer's rule)

$$x_i = \frac{\det(A_i)}{\det(A)}$$

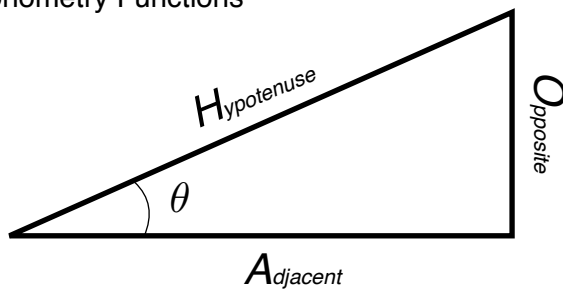
Forms of a 2nd order polynomial

$$y = ax^2 + bx + c$$

$$y = a(x - h)^2 + k$$

$$y = (x - m)(x - n)$$

### Trigonometry Functions



$$\sin(\theta) = \frac{O}{H} \quad \sin^{-1}\left(\frac{O}{H}\right) = \theta$$

$$\cos(\theta) = \frac{A}{H} \quad \cos^{-1}\left(\frac{A}{H}\right) = \theta$$

$$\tan(\theta) = \frac{O}{A} \quad \tan^{-1}\left(\frac{O}{A}\right) = \theta$$

### Pythagoras Theorem

$$H^2 = O^2 + A^2$$

### Unit Conversions

angles

$$2\pi = 6.28 \text{ rad} = 360^\circ$$

mass

$$1 \text{ kg} = 2.2 \text{ lbs.}$$

lengths

$$1 \text{ mile} = 1.6 \text{ km}$$

$$1 \text{ inch} = 2.54 \text{ cm}$$

$$1 \text{ m} = 3.3 \text{ ft}$$

volumes

$$1 \text{ gallon} = 3.78 \text{ Litres}$$

(4 marks) Match the “type of number” with the best “example number”. Draw a line to match the “type of number” to the “example number” to indicate your answer.

rational	$-\sqrt{2}$
integer	$-2.2$
natural	$-2$
irrational	$+2$

(3 marks) Determine

- the total number of significant digits and
- re-write the number in scientific notation

for the following number:

2030                      a) significant digits = \_\_\_\_\_

b) scientific notation = \_\_\_\_\_

0.0002030                a) significant digits = \_\_\_\_\_

b) scientific notation = \_\_\_\_\_

0.2                         a) significant digits = \_\_\_\_\_

b) scientific notation = \_\_\_\_\_

(6 marks) Given the standard unit conversion table on the formula sheet (1st page), convert each of the numbers to the stated units.

$$4.3 \frac{\text{lbs.}}{\text{minute}} \rightarrow \frac{\text{kg}}{\text{hour}}$$

$$0.0043 \frac{\text{mile}}{\text{hour}} \rightarrow \frac{\text{km}}{\text{second}}$$

$$8.34 \frac{\text{inch}}{\text{gallon}^2} \rightarrow \frac{\text{cm}}{\text{L}^2}$$

$$2.1 \frac{\text{kg}}{\text{L}} \rightarrow \frac{\text{lbs.}}{100 \text{ mL}}$$

(12 marks) Solve for x in the following equation.

$$2x - 6.2 = 5$$

$$4ax - b^a = c$$

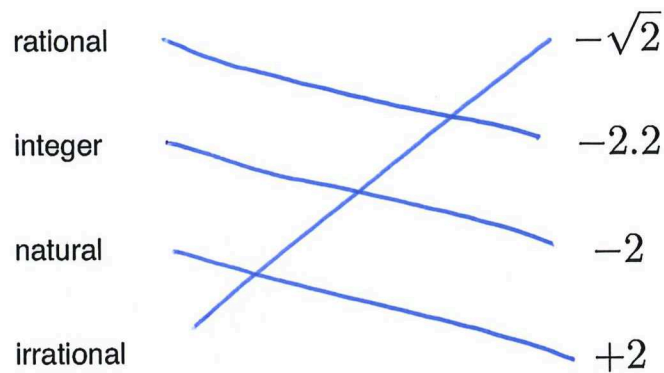
$$3x^2 + 1 = 13.1$$

$$\frac{1}{x} = \frac{a}{4b}$$

$$\log(x) - 1 = 1.2$$

$$10^x = 2385.4$$

(4 marks) Match the "type of number" with the best "example number". Draw a line to match the "type of number" to the "example number" to indicate your answer.



(3 marks) Determine

- the total number of significant digits and
- re-write the number in scientific notation

for the following number:

2030

a) significant digits = 3

b) scientific notation =  $2.03 \times 10^3$

0.0002030

a) significant digits = 4

b) scientific notation =  $2.030 \times 10^{-4}$

0.2

a) significant digits = 1

b) scientific notation =  $2 \times 10^{-1}$

(6 marks) Given the standard unit conversion table on the formula sheet (1st page), convert each of the numbers to the stated units.

$$4.3 \frac{\text{lbs.}}{\text{minute}} \rightarrow \frac{\text{kg}}{\text{hour}}$$

$$4.3 \frac{\cancel{\text{lbs.}}}{\cancel{\text{min}}} \left( \frac{1 \text{ kg}}{2.2 \cancel{\text{ lbs}}} \right) \left( \frac{60 \cancel{\text{ min}}}{1 \text{ hour}} \right) = 117.3 \frac{\text{kg}}{\text{hour}}$$

$$= \boxed{120 \frac{\text{kg}}{\text{hour}}}$$

$$0.0043 \frac{\text{mile}}{\text{hour}} \rightarrow \frac{\text{km}}{\text{second}}$$

$$0.0043 \frac{\cancel{\text{mile}}}{\cancel{\text{hour}}} \left( \frac{1.6 \text{ km}}{1 \cancel{\text{ mile}}} \right) \left( \frac{1 \cancel{\text{ hour}}}{60 \cancel{\text{ min}}} \right) \left( \frac{1 \cancel{\text{ min}}}{60 \text{ sec}} \right) = 1.91 \times 10^{-6} \frac{\text{km}}{\text{sec}}$$

$$= \boxed{1.9 \times 10^{-6} \frac{\text{km}}{\text{sec}}}$$

$$8.34 \frac{\text{inch}}{\text{gallon}^2} \rightarrow \frac{\text{cm}}{\text{L}^2}$$

$$8.34 \frac{\cancel{\text{inch}}}{\cancel{\text{gallon}^2}} \left( \frac{2.54 \text{ cm}}{1 \cancel{\text{ inch}}} \right) \left( \frac{1 \cancel{\text{ gallon}}}{3.78 \text{ L}} \right) \left( \frac{1 \cancel{\text{ gallon}}}{3.78 \text{ L}} \right) = 1.48 \frac{\text{cm}}{\text{L}^2}$$

$$= \boxed{1.48 \frac{\text{cm}}{\text{L}^2}}$$

$$2.1 \frac{\text{kg}}{\text{L}} \rightarrow \frac{\text{lbs.}}{100 \text{ mL}}$$

$$2.1 \frac{\cancel{\text{kg}}}{\cancel{\text{L}}} \left( \frac{2.2 \text{ (lbs)}}{1 \cancel{\text{ kg}}} \right) \left( \frac{1 \cancel{\text{ L}}}{1000 \cancel{\text{ mL}}} \right) \left( \frac{100 \cancel{\text{ mL}}}{100 \text{ mL}} \right) = 0.462 \frac{\text{lbs}}{100 \text{ mL}}$$

$$= \boxed{0.46 \frac{\text{lbs}}{100 \text{ mL}}}$$

(12 marks) Solve for x in the following equation.

$$2x - 6.2 = 5$$

$$\frac{2x}{2} = \frac{11.2}{2}$$

$$x = 5.6$$

$$4ax - b^a = c$$

$$\frac{4ax}{4a} = \frac{c + b^a}{4a}$$

$$x = \frac{c + b^a}{4a}$$

$$3x^2 + 1 = 13.1$$

$$\frac{3x^2}{3} = \frac{12.1}{3}$$

$$\sqrt{x^2} = \sqrt{4.0\bar{3}}$$

$$x = 2.008$$

$$4bx \left( \frac{1}{x} \right) = \left( \frac{a}{4b} \right) 4bx$$

$$\frac{4b}{a} = \frac{ax}{a}$$

$$x = \frac{4b}{a}$$

$$\log(x) - 1 = 1.2$$

$$\log(x) = 2.2$$

$$10^{\log(x)} = 10^{2.2}$$

$$x = 158.5$$

$$10^x = 2385.4$$

$$\log(10^x) = \log(2385.4)$$

$$x = 3.378$$

Instructor:	Frank Secretain
Course:	Math 150
Date:	May 21, 2025
Assessment:	Test 1 (practice)
Time allowed:	110 minutes
Devices allowed:	Pencil, pen, eraser, calculator
Notes from instructor:	Be neat. Show your work where needed. Box final answers.
Marks allocated:	4 questions worth 25 marks
Percentage of final grade:	25% of final grade

## Formula Sheet

### Order of Operations

$$ac + bc = c(a + b)$$

exponents

$$a^n a^m = a^{n+m}$$

$$(a^n)^m = a^{nm}$$

$$(ab)^n = a^n b^n$$

$$a^0 = 1$$

$$a^{-n} = \frac{1}{a^n}$$

radicals

$$a^{\frac{n}{m}} = \sqrt[m]{a^n}$$

### Relative Velocity

$$\vec{v}_{\frac{A}{C}} = \vec{v}_{\frac{A}{B}} + \vec{v}_{\frac{B}{C}}$$

Linear equations (Cramer's rule)

$$x_i = \frac{\det(A_i)}{\det(A)}$$

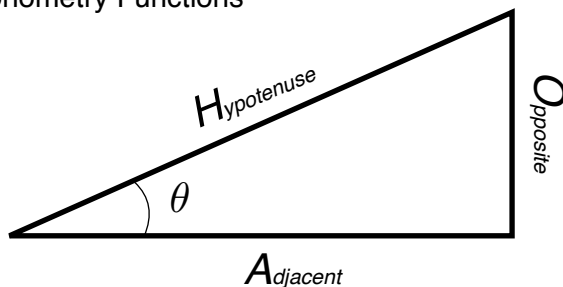
Forms of a 2nd order polynomial

$$y = ax^2 + bx + c$$

$$y = a(x - h)^2 + k$$

$$y = (x - m)(x - n)$$

### Trigonometry Functions



$$\sin(\theta) = \frac{O}{H} \quad \sin^{-1}\left(\frac{O}{H}\right) = \theta$$

$$\cos(\theta) = \frac{A}{H} \quad \cos^{-1}\left(\frac{A}{H}\right) = \theta$$

$$\tan(\theta) = \frac{O}{A} \quad \tan^{-1}\left(\frac{O}{A}\right) = \theta$$

### Pythagoras Theorem

$$H^2 = O^2 + A^2$$

### Unit Conversions

angles

$$2\pi = 6.28 \text{ rad} = 360^\circ$$

mass

$$1 \text{ kg} = 2.2 \text{ lbs.}$$

lengths

$$1 \text{ mile} = 1.6 \text{ km}$$

$$1 \text{ inch} = 2.54 \text{ cm}$$

$$1 \text{ m} = 3.3 \text{ ft}$$

volumes

$$1 \text{ gallon} = 3.78 \text{ Litres}$$

(4 marks) Match the “type of number” with the best “example number”. Draw a line to match the “type of number” to the “example number” to indicate your answer.

irrational	0
integer	$-\sqrt{1}$
rational	-2.1
whole	$\sqrt{3}$

(3 marks) Determine

- the total number of significant digits and
- re-write the number in scientific notation

for the following number:

50200                      a) significant digits = \_\_\_\_\_

b) scientific notation = \_\_\_\_\_

0.020310                      a) significant digits = \_\_\_\_\_

b) scientific notation = \_\_\_\_\_

0.70                              a) significant digits = \_\_\_\_\_

b) scientific notation = \_\_\_\_\_

(6 marks) Given the standard unit conversion table on the formula sheet (1st page), convert each of the numbers to the stated units.

$$3.2 \frac{\text{kg}}{\text{second}} \rightarrow \frac{\text{lbs.}}{\text{minute}}$$

$$0.0452 \frac{\text{radians}}{\text{inch}} \rightarrow \frac{\text{degrees}}{\text{m}}$$

$$0.00873 \frac{\text{gallon}^2}{\text{minute}} \rightarrow \frac{\text{Litres}^2}{\text{day}}$$

$$954 \frac{\text{kg}}{\text{L}} \rightarrow \frac{\text{lbs}}{100 \text{ mL}}$$

(12 marks) Solve for  $x$  in the following equation.

$$4x - 8.3 = 2$$

$$4ax - c = b$$

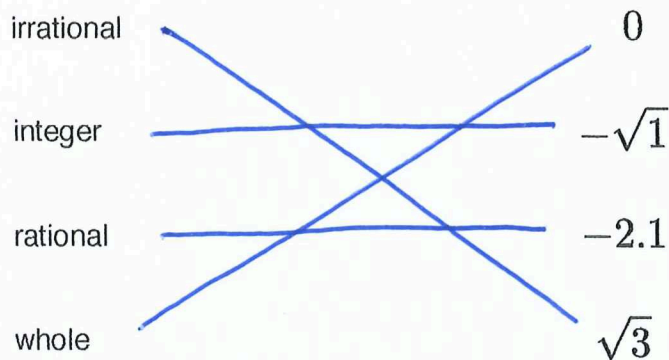
$$5x = \frac{a}{4b}$$

$$\frac{1}{3x} = \frac{a}{2c}$$

$$3x^2 - 1 = b + 2$$

$$\log(x) = 0.0342$$

(4 marks) Match the "type of number" with the best "example number". Draw a line to match the "type of number" to the "example number" to indicate your answer.



(3 marks) Determine

- the total number of significant digits and
- re-write the number in scientific notation

for the following number:

50200

a) significant digits = 3

b) scientific notation =  $5.02 \times 10^4$

0.020310

a) significant digits = 5

b) scientific notation =  $2.0310 \times 10^{-2}$

0.70

a) significant digits = 2

b) scientific notation =  $7.0 \times 10^{-1}$

(6 marks) Given the standard unit conversion table on the formula sheet (1st page), convert each of the numbers to the stated units.

$$3.2 \frac{\text{kg}}{\text{second}} \rightarrow \frac{\text{lbs.}}{\text{minute}}$$

$$3.2 \frac{\cancel{\text{kg}}}{\cancel{\text{s}}} \left( \frac{2.2 \text{ lbs}}{\cancel{1 \text{ kg}}} \right) \left( \frac{\cancel{60 \text{ s}}}{1 \text{ min}} \right) = 422.4 \frac{\text{lbs}}{\text{min}} = 420 \frac{\text{lbs}}{\text{min}}$$

$$0.0452 \frac{\text{radians}}{\text{inch}} \rightarrow \frac{\text{degrees}}{\text{m}}$$

$$0.0452 \frac{\cancel{\text{rads}}}{\cancel{\text{inch}}} \left( \frac{360 \text{ deg}}{\cancel{6.28 \text{ rad}}} \right) \left( \frac{1 \cancel{\text{ inch}}}{2.54 \cancel{\text{ cm}}} \right) \left( \frac{100 \cancel{\text{ cm}}}{1 \text{ m}} \right) = 102.01 \frac{\text{deg}}{\text{m}}$$

$$= 102 \frac{\text{deg}}{\text{m}}$$

$$0.00873 \frac{\text{gallon}^2}{\text{minute}} \rightarrow \frac{\text{Litres}^2}{\text{day}}$$

$$0.00873 \frac{\cancel{\text{gallon}^2}}{\cancel{\text{minute}}} \left( \frac{3.78 \text{ L}}{\cancel{1 \text{ gal}}} \right) \left( \frac{3.78 \text{ L}}{\cancel{1 \text{ gal}}} \right) \left( \frac{\cancel{60 \text{ min}}}{1 \cancel{\text{ hour}}} \right) \left( \frac{\cancel{24 \text{ hour}}}{1 \text{ day}} \right) = 179.62 \frac{\text{L}^2}{\text{day}}$$

$$= 1.80 \frac{\text{L}^2}{\text{day}}$$

$$954 \frac{\text{kg}}{\text{L}} \rightarrow \frac{\text{lbs}}{100 \text{ mL}}$$

$$954 \frac{\cancel{\text{kg}}}{\cancel{\text{L}}} \left( \frac{2.2 \text{ lbs}}{\cancel{1 \text{ kg}}} \right) \left( \frac{1 \cancel{\text{ L}}}{1000 \cancel{\text{ mL}}} \right) \left( \frac{100 \cancel{\text{ mL}}}{100 \text{ mL}} \right) = 209.88 \frac{\text{lbs}}{100 \text{ mL}}$$

$$= 2.10 \frac{\text{lbs}}{100 \text{ mL}}$$

(12 marks) Solve for x in the following equation.

$$4x - 8.3 = 2$$

$$\frac{4x}{4} = \frac{10.3}{4}$$

$$x = 2.575$$

$$4ax - c = b$$

$$\frac{4ax}{4a} = \frac{b+c}{4a}$$

$$x = \frac{b+c}{4a}$$

$$\frac{1}{5} (5x) = \left(\frac{a}{4b}\right) \frac{1}{5}$$

$$x = \frac{a}{20b}$$

$$(\cancel{2c})(\cancel{3x}) \left( \frac{1}{\cancel{3a}} \right) = \left( \frac{a}{\cancel{2c}} \right) (\cancel{3x})(\cancel{2c})$$

$$\frac{2c}{3a} = \frac{\cancel{3a}x}{\cancel{3a}}$$

$$\frac{2c}{3a} = x$$

$$x = \frac{2c}{3a}$$

$$3x^2 - 1 = b + 2$$

$$\frac{\cancel{3}x^2}{\cancel{3}} = \frac{b+3}{3}$$

$$\sqrt{x^2} = \sqrt{\frac{b+3}{3}}$$

$$x = \sqrt{\frac{b+3}{3}}$$

$$\log(x) = 0.0342$$

$$10^{\log(x)} = 10^{0.0342}$$

$$x = 1.082$$