

Decimal to Fraction (terminating)

$$0.1 = 0.1(1) = \frac{0.1}{1} \left(\frac{10}{10} \right) = \frac{1}{10}$$

$$0.3 = 0.3 \left(\frac{10}{10} \right) = \frac{3}{10}$$

$$0.5 = 0.5 \left(\frac{10}{10} \right) = \frac{5}{10} \left(\frac{\div 5}{\div 5} \right) = \frac{1}{2}$$

$$0.65 = 0.65 \left(\frac{100}{100} \right) = \frac{65}{100} \left(\frac{\div 5}{\div 5} \right) = \frac{13}{20}$$

$$0.75 = 0.75 \left(\frac{100}{100} \right) = \frac{75}{100} \left(\frac{\div 5}{\div 5} \right) = \frac{15}{20} \left(\frac{\div 5}{\div 5} \right) = \frac{3}{4}$$

$$0.758 = 0.758 \left(\frac{1000}{1000} \right) = \frac{758}{1000} \left(\frac{\div 2}{\div 2} \right) = \frac{379}{500}$$

$$0.2348 = 0.2348 \left(\frac{10000}{10000} \right) = \frac{2348}{10000} \left(\frac{\div 2}{\div 2} \right) = \frac{1174}{5000} \left(\frac{\div 2}{\div 2} \right) = \frac{587}{2500}$$

Decimal to fraction (repeating)

$$0.\overline{3} = \frac{1}{3}$$

$$0.\overline{6} = \frac{2}{3}$$

$$0.\overline{7} \quad \text{let } x = 0.777\dots \quad \text{so} \quad \begin{array}{r} 10x = 7.7777\dots \\ - x = 0.7777\dots \\ \hline 9x = 7 \end{array} \quad \text{so} \quad x = \frac{7}{9}$$

$$0.\overline{23} \quad \text{let } x = 232323\dots \quad \text{so} \quad \begin{array}{r} 100x = 23.2323\dots \\ - x = 0.2323\dots \\ \hline 99x = 23 \end{array} \quad \text{so} \quad x = \frac{23}{99}$$

$$0.2\overline{83} \quad \text{let } \begin{array}{l} y = 0.28 \\ x = 0.00333\dots \end{array} \quad \text{so} \quad \begin{array}{r} 10x = 0.03333\dots \\ - x = 0.00333\dots \\ \hline 9x = 0.03 \end{array} \quad \text{so} \quad \begin{array}{l} y = \frac{28}{100} = \frac{252}{900} \\ x = \frac{0.03}{9} = \frac{3}{900} \end{array} \quad \left. \begin{array}{l} \diagdown \\ \diagup \end{array} \right\} \frac{255}{900} = \frac{17}{60}$$

$$0.4\overline{47} \quad \text{let } \begin{array}{l} y = 0.44 \\ x = 0.00777\dots \end{array} \quad \text{so} \quad \begin{array}{r} 10x = 0.07777\dots \\ - x = 0.00777\dots \\ \hline 9x = 0.07 \end{array} \quad \text{so} \quad \begin{array}{l} y = \frac{44}{100} = \frac{396}{900} \\ x = \frac{0.07}{9} = \frac{7}{900} \end{array} \quad \left. \begin{array}{l} \diagdown \\ \diagup \end{array} \right\} \frac{403}{900}$$

$$0.3\overline{287} \quad \text{let } \begin{array}{l} y = 0.32 \\ x = 0.008787\dots \end{array} \quad \text{so} \quad \begin{array}{r} 100x = 0.878787\dots \\ - x = 0.008787\dots \\ \hline 99x = 0.87 \end{array} \quad \text{so} \quad \begin{array}{l} y = \frac{32}{100} = \frac{3168}{9900} \\ x = \frac{0.87}{99} = \frac{87}{9900} \end{array} \quad \left. \begin{array}{l} \diagdown \\ \diagup \end{array} \right\} \frac{3255}{9900} = \frac{217}{660}$$